

Complete the following:

p. 675 - 676

#17: complete a test (\neq)
and then an appropriate conf. interval

$H_0: \beta_1 = 0$

$H_a: \beta_1 \neq 0$

Conditions:

- | | |
|--------------------------------|---|
| 1) S R S | 1) assumed representative |
| 2) l inear data | 2) scatterplot is linear |
| 3) i ndependent | 3) each car is indep. of the others |
| 4) N ormal resid. | 4) histogram of the residuals is symmetric, unimodal |
| 5) E qual variance | 5) the residual plot shows no change in the spread of the residuals |

conditions met --> t-distribution --> LinReg T test

$$t = \frac{-8.21362}{0.6738} = -12.2 \quad (\text{or } -12.19)$$

$$P(t < -12.2) = 0 \quad df = 48$$

We reject H_0 b/c the p-value of $0 < \alpha = 0.05$.

We have sufficient evidence that the slope of the population regression line is not equal to 0.

Therefore, as weight of a car increases, the fuel efficiency (mpg) changes.

95% confidence interval: $df = 48$

Conditions met, t distribution, LinReg t Interval

$$-8.21362 \pm (2.0106)(0.6738) = (-9.56832, -6.85892)$$

We are 95% confident that for every increase of 1000 lbs of a car's weight, the fuel efficiency decreases between 6.859 mpg and 9.568 mpg.

Ch. 27 Part 2

Using Actual data to test the slope

Example: Airfare Data (Dist vs. Airf)

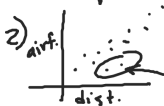

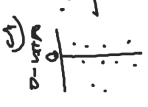
Test to see if the slope of the pop. regr. line between distance and airfare is positive.

Hypotheses:

$$H_0: \beta_1 = 0$$

$$H_a: \beta_1 > 0$$

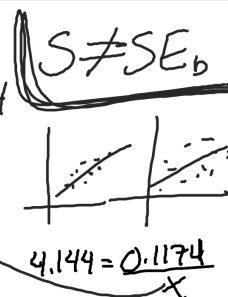
Conditions:

- 1) SRS
 - 2) Linear data
 - 3) Indep.
 - 4) Normal resid.
 - 5) Equal Variance
- Conditions met
t distrib.
Lin Reg t test
- 1) Assume flights are representative
 - 2)  Scatterplot linear, 2 poss. outliers
 - 3) Assume flights are indep. of each other.
 - 4)  Normal prob. plot is linear → normal resid.
 - 5)  Resid plot is scattered

Mechanics:

Test Stat:

$$t = \frac{b_1}{SE_{b_1}} = \frac{0.1174}{0.0283} = 4.144$$



P-Value

$$P(t > 4.144) = 9.993 \times 10^{-4}$$

df = 10

Conclusion:

Confidence Interval:

$$\text{Conf} = 90\% \quad df = 10$$

cond. met, t distrib, Lin Reg t Interval

$$0.1174 \pm (1.8125)(0.0283)$$

$$= (0.06604, 0.16871)$$

Practice:

p. 675 #14 & 16

p. 679 #34- do not do letter (a)

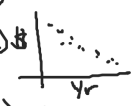
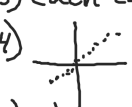
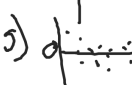
14)

$$H_0: \beta_1 = 0$$

$$H_a: \beta_1 < 0$$

p. 675

Conditions:

- 1) SRS
 - 2) Linear data
 - 3) Indep.
 - 4) Normal resid
 - 5) Equal var.
- 1) assume cars are representative.
 - 2)  Scatterplot is linear
 - 3) Each car is indep. of others
 - 4)  normal prob. plot is linear → normal resid.
 - 5)  resid plot is mostly scattered.

Cond. met, t distrib, LinReg ttest

$$t = \frac{b_1}{SE_{b_1}} = \frac{-959.05}{64.582} = -14.85$$

$$P(t < -14.85) = 7.8118 \times 10^{-10}$$

df = 13

$-14.85 = \frac{-959.05}{x}$

- Reject H_0 ...
- slope of pop. reg. line < 0 .
- Therefore as age of car increases, price decr.

$\alpha = 0.05$
 $H_a: <$
 $C = 90\%$
 $df = 13$

INVT
 $N = ? 14$
 $C = 2.90$

Cond. met, t distrib, Lin Reg t Int.

$$b_1 \pm (t^*) (SE_{b_1})$$

$$-959.05 \pm (1.771)(64.582)$$

$$= (-1073, -844.70)$$

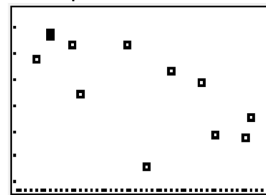
We are 90% conf. that for every year older the car gets, the price decreases btw. \$844.70 and \$1073.

invT(0.05, 13)

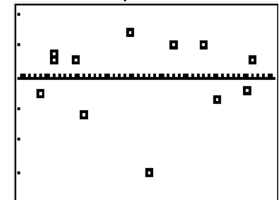
p. 679 #34- do not do letter (a)

- ① type in data
- ② LinReg(ax+b) L_1, L_2

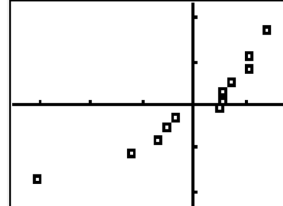
Scatterplot:



Resid plot:



Normal prob plot



Lin Reg T test

```
LinRegTTest
y=a+bx
B<0 and P<0
t=-3.097142482
P=.0056527767
df=10
a=35.67805955
```

34) (b) $H_0: \beta_1 = 0$
 $H_a: \beta_1 < 0$

Conditions:

- | | |
|-------------------|---|
| 1) SRS | 1) assumed representative |
| 2) linear data | 2) scatterplot is linear, one poss. outlier |
| 3) independent | 3) each baby is indep. of the others |
| 4) normal resid. | 4) normal prob. plot of resid. is roughly linear --> normal data |
| 5) Equal variance | 5) the residual plot shows no change in the spread of the residuals (poss. outlier) |

conditions met --> t-distribution --> LinReg T test

$$t = \frac{-0.0778}{0.02512} = -3.097$$

$$-3.097 = \frac{-0.0778}{SE_b}$$

$$P(t < -3.097 | df = 10) = 0.00565$$

We reject H_0 b/c p-value of 0.00565 < $\alpha = 0.05$.

We have sufficient evidence that the slope of the population regression line between 6-month temp & avg. crawling age is less than 0.

Thus as 6 month temperature increases, average crawling age decreases.

(c) conditions met --> t distribution --> LinReg t-Interval

$$-0.0778 \pm (2.228)(0.02512) = (-0.13377, -0.02183)$$

We are 95% confident that for every increase in 1 degree of the average 6 month temperature, the average crawling age decreases between 0.02183 and 0.13377 weeks.